

Fast Multi-Scaled Texture Generation and Rendering

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Abstract

The multi-scaled model for stochastic texture representation and the method providing real-time rendering of textures formalized by this model are introduced. Both “abstract” and “natural-like” textures can be generated. Being much simpler than existing stochastic texture models it satisfies the requirements of real-time texture mapping: compact data representation, scalability, random pixel access. The rendering algorithm is simple enough to be implemented in hardware.

Keywords: *stochastic textures, texture mapping, multi-scaled representation, wavelet transform*

1. INTRODUCTION

At least two objects are usually referred to as textures. First is an ordinary image processed and stored in a way convenient for mapping purpose [6], e.g. image of a palace facade to be mapped to the corresponding geometry to create a realistic 3D model of the building. Storing such a texture in explicit form is expensive (as hundreds of textures are to be stored in graphical device memory simultaneously) so the image is to be compressed. Texture compression methods have to satisfy some special requirements. In particular, the decompression algorithm must be as much simple and fast as possible and suitable for implementation in hardware. Then it must provide random access or local reconstruction, i.e. the ability to evaluate an arbitrary pixel of the image without reconstruction of the whole object. Moreover, a texture is to be represented in a way convenient for mapping on different resolution levels. This is usually achieved by *mip-mapping*, i.e. storing the sequence of 1:2, 1:4, 1:8, etc., scaled copies in addition to the initial image.

Another object is texture in its initial meaning, i.e. texture of material (wood, paper, marble, textile, etc.), texture of sandy, or water, or ground surfaces, texture of leather and soon. Also different “abstract” patterns can be treated as textures.

Such textures are usually processed in the following way. Given a relatively small sample of a texture, it is to be spread over any desired size. The easiest way is simple tiling of the initial sample, but this produces poor results as it leads to periodic effect that looks unnatural.

There exist several *stochastic models* [1][3][4] to represent such textures. All of them are based on the hypothesis that textures can be formalized as probabilistic distributions. A texture sample is a sample from such a distribution. It should be analyzed in an attempt to capture the distribution. If distribution is found properly, then the initial sample and image, generated according to the distribution, must be perceived as two samples of the same texture, though not the same images.

In [1][2] the iteration method is used for texture synthesis and analysis: the inputs are texture and random noise samples, they are sequentially converted to the texture image of desired size. In [3] the Laplacian pyramid is built to analyze texture sample, on the synthesis phase the pyramid is transformed in a way preserving high-resolution features (deterministic component) and affecting low-resolution features (probabilistic component). In [4] textures are modeled as Markov Random Fields.

The idea to represent a texture with a small object containing all the information necessary for generation looks attractive, as this representation is sufficiently compact. Moreover, the size of such a representation doesn't depend on size of the output. Unfortunately, generation of textures from a small object is not suitable for real-time applications. All the techniques mentioned above require sufficiently complicated and time-consuming calculations. Thus if real-time texture mapping is required, the image of the desired size is to be generated before the rendering phase and then stored using texture compression techniques which do not take into account the special structure of the image.

Our task was to find a model for texture representation, which is probably not so powerful as existing models are, but satisfying the requirements of real-time texture mapping, mentioned above.

First a method for fast creation of new artificial textures was developed. The idea was to take some trivial image (base element) composed by a user in a minute by means of simple graphical editor and to generate a new image from randomly scattered scaled and rotated copies of base element.

The next step was to modify a model in a way providing realistic approximation of some natural textures.

On the third step the compact texture data representation and fast rendering algorithm was developed.

The remainder of the paper is organized as follows. Section 2 contains the detailed description of the texture representation model. Some examples and results are introduced in Section 3. In Section 4 the proposed model is compared with wavelet transform of images. Section 5 introduces Layer Control Masks, the effective rendering technique. In Section 6 some implementation details and estimation of calculation complexity and data size are also discussed. The concluding Section 7 contains some ideas on model enhancement and the proposal for further research.

2. THE MODEL DESCRIPTION

As it was mentioned above, the idea behind the model was to compose an object from randomly scattered scaled and rotated copies of some small and simple trivial image (*base element*). In practice, however, not all the possible scales and rotations of

baseelementareused;thelacethecopyofbaseelementcanbe droppedtoisnotabsolutelyrandomalso.

2.1 Replications

The *replication* is one copy (may be scaled and transformed as described below) of baseelement to be placed to output image. The point of output image is called *replication point* if it has non-zero probability to be the origin of one of the replications.

Assume then that the baseelement is a square bitmap with side size $N = 2^K$ pixels. Then the scaled versions of the element are also squared bitmaps with side size 2^k , $k = 1, \dots, K$. Index k is called *resolution level* or *resolution*.

Elements can be replicated with shift equal to one half of their side size. That means that on the resolution level k , which corresponds to image side size 2^k , the replication points are $(2^{k-1}i, 2^{k-1}j)$, $i, j \in \mathbf{Z}$.

In each replication point the following *events* can take place:

- Baseelement can be replicated (*positive replication*), or negative of the baseelement can be replicated (*negative replication*), or baseelement can be not replicated at all (*no replication*).
- Baseelement can be *rotated* to 90° , 180° and 270° , or not rotated, (i.e. rotated to 0°).
- Baseelement can be *mirrored* or not mirrored.

For the particular model one can specify the probability of each of these events.

2.2 Composing Image from Replications

We assume that baseelements can have pixels with both positive and negative intensity. Baseelement background has zero intensity and is considered to be “transparent”.

At the initial step the output image is the rectangular of desired size with zero intensity.

Then replications of baseelement are placed to the output image. The element can be simply added, but other operations are available.

Assume that a is the current intensity value of some pixel of output image, b is the pixel value of a replication which is to update a and \tilde{a} is the updated intensity of the pixel. Then the following operations are available:

- simple addition

$$\tilde{a} = a + b.$$

- non-zero application

$$\tilde{a} = \begin{cases} a, & b = 0 \\ b, & b \neq 0 \end{cases}$$

- “maximum” application

$$\tilde{a} = \begin{cases} a, & |a| \geq |b| \\ b, & |a| < |b| \end{cases}$$

The two latter operations are not linear, and not commutative, i.e. their result is dependent on the order of replication. This feature can be used to control “transparency” of replications.

The probability of choice of one of these operations for each replication can be also specified.

Replications of equal resolution form *layers* of output image. One *weight coefficient* can be assigned to each layer. In this case all the replications of the layer are to be multiplied by the corresponding coefficient. This controls the contrast of the layer and consequently the layer significance in output image. Note that the terms *resolution level* and *layer* are closely connected with each other, but they are not equivalent (see Section 2.4 below).

The order of replication can be different. One of the easiest ways is *layer-to-layer* order. It is possible to specify whether to move from top level to bottom or vice versa.

The final step of the generation is adding some “background” intensity value to each pixel of an image.

2.3 Model Parameters Specification

To create a particular model one has to specify number of layers and table of probabilistic distribution of event taking place in replication points of each level (*event tables*).

In the simplest case event table has only one cell. It means that the only distribution is used for all the replication points of a layer. The polar situation is when the particular distribution is specified for each replication point, but this seems to have no sense. Usually event table determines the event probabilities for a group of several neighbour replication points.

As to the baseelement it can be either included or not included in model specification. The latter case means that the model was intended to be used with different baseelements.

Such parameters as background intensity of the whole image, weight coefficients for each layer and order of generation (top to bottom or bottom to top) are to be specified also.

2.4 Scaling

The proposed model provides the easy way to generate 1:2, 1:4, 1:8, etc., scaled copies of textures. Indeed, by default the top layer (layer 0) corresponds to resolution K of baseelement, layer 1 corresponds to resolution $(K - 1)$, etc. If to shift this correspondence (e.g. layer 0 to resolution $(K - 1)$, layer 1 to resolution $(K - 2)$, etc.) then scaled (reduced) version of the texture will be generated. It is also possible to magnify the texture (e.g. layer 0 corresponds to resolution $(K + 1)$), but in this case the baseelement is to be stretched to resolutions higher than K .

3. EXAMPLES

Random Rotation Model

The simplest model is called “random rotation”. The 2×2 event table consists of two staggered zero entries (which correspond to “no replication” with probability 1), the two remaining entries are the same and specify the uniform distribution of rotation angle (Tab. 1). The table is the same for any layer. The number of layers can be different but usually is 3 or 4. Weight coefficients can be different also but in the simplest case they all are equal to 1.

The base element is not specified. Originally this very model was used to generate new textures. So the model except the base element was pre-defined for a user could compose new base elements for it.

Instead of “negative application” the following pre-processing of base elements was used for this model: the base element was summarized with its mirrored and inverted copy. The mean of such a pre-processed element is always 0.

Examples of textures, generated by “random rotation” model are shown on Fig. 1 (corresponding base elements are replaced to top left corner of each image, the left most texture is presented in two scales).

Cheese

The “cheese” is a simple example of natural texture approximation. The more or less realistic model of cheese is just a number of holes scattered along a plane. Holes can be of different size, their shape and orientation are arbitrary. There must not be too many holes, so the probability of a hole replication must not be very high. We simplified this model by using the only shape for all the holes (Fig. 2, left) and only two scales. Nevertheless, the result looks like a piece of cheese (Fig. 2, right).

Brick Wall

The brick wall appeared to be an interesting example. The “ideal” brick wall is a regular structure, and can be represented easily. The task was to add some sort of irregularity to make the result look more natural. The “half brick” image was used as the base element (Fig. 3, left). In the ideal case each two elements in any row are to be 180° rotated copies of each other, and two neighbouring rows are to be shifted copies of each other. We affected this order by adding a small probability for the element to be oriented not in the proper way. One of the possible distributions is introduced in Tab. 3. The result is shown on Fig. 3, center. The “realism” of the image can be increased by adding some sort of noise (Fig. 3, right). This noise is just the very base element replicated with a low weight coefficient (0.2) on layers 2 and 3 according to some uniform distribution (Tab. 2).

4. CONNECTION WITH WAVELET THEORY

One can notice that the introduced model looks similar to image wavelet synthesis [7] (i.e. inverse wavelet transform) and so called *random wavelet expansion*, introduced in [5].

Here is the well-known formula of 2D dyadic wavelet reconstruction:

$$I(x, y) = v \varphi(x, y) + \sum_{k=0}^K \sum_{i,j=-\infty}^{+\infty} w_{ij}^{(k)} \psi(2^k x - i, 2^k y - j)$$

Suppose now that base element is another wavelet $\psi(\bullet, \bullet)$ (as it was mentioned above, in some experiments base elements were pre-processed to satisfy at least one attribute of the real wavelet, i.e. to have zero mean). Instead of wavelet coefficient $w_{ij}^{(k)}$, weight coefficient $w^{(k)}$, which is one per resolution k , is used. Each scaled and shifted copy of $\psi(\bullet, \bullet)$ is transformed (rotated, inverted, etc., or simply vanished) by the functional $\mathbf{W}[\bullet, \xi]$. The functional is controlled by random variable ξ which distribution depends, in general, on layer k and space disposition. The “low-resolution” part is expressed by the mean intensity v . Thus we get the following formula:

$$I(x, y) = v + \bigoplus_{k=0}^K \bigoplus_{i,j=-\infty}^{+\infty} w^{(k)} \mathbf{W}[\psi(2^k x - i, 2^k y - j), \xi_{ij}^{(k)}]$$

Symbols \bigoplus are used instead of \sum to show that operations similar but not identical to addition can be used. (Note that in general the choice of the operation is also controlled by a random variable).

The main common feature of both formulas is that they represent an object $I(\bullet, \bullet)$ as a collection of scaled and shifted copies of some element $\psi(\bullet, \bullet)$. And, consequently, both expressions provide good scalability.

5. LAYER CONTROL MASK

For texture mapping purpose it is desirable not to generate a texture as the whole image, but to calculate small patches or even single pixels of the texture (*local generation*). The generation scheme described above is badly suitable for local generation as it uses random-number generator. Indeed, all the instances of a texture generated according to some model are samples from the same probabilistic distribution, but they are not the same image. In case of local generation different patches or pixels belong to different samples, i.e. they do not belong to the same images. Even two attempts to calculate one particular pixel can give two different results.

So the problem is to find a technique that guarantees that all the locally generated patches or pixels belong to the same image.

One of the possible solutions is to calculate the events in each replication point *before* the generation phase started and to store the results in special data structures.

Since in the proposed model the layers are regenerated independently from each other, the structure storing pre-calculated events is actually a set of 2-dimensional arrays. Each array corresponds to one layer. Each entry of an array corresponds to one replication point and contains a code describing replication event in this point. Such an array is called *layer control mask* (LCM).

Notethatonlyonebyteisenoughtocodeallthepossibleevents. Indeed,2bitsarenecessarytocodepositive/negative/none replication,2bitsforthe four possible rotation angles,1bitfor mirroringand2bitstocodethereplicationoperation.Sevenbits total.

LCMsprovidesbothglobalandlocalgeneration.Global generationisperformedinnearlythesamewayasdescribed above,thelonlydifferenceisthatthegeneratorusesprepared eventcodesinsteadofcomputingthem.Forlocalgenerationnot alltheentriesofLCMsareusedbutonlythosecorrespondedto specifiedspatialarea.

OnecanseethattheuseofLCMsnotonlysolvethetheproblemof localgeneration butalsosplitsthegenerationprocessintotwo phases:(a)LCMgenerationand(b)texturerenderingusing preparedLCMs.Notethatonlythesecondphaseisessentialto bereal-time.TheLCMgenerationcontainsthemainpartof necessarycalculations.Actuallythesecalculationsarenotvery complicatedinexistingmodel,butifthemodelisenhanced(see Section 7.1)thecalculationswillbecomemoresophisticatedand time-consuming.Moreover,thedescriptionofthamodel(and hencetheinputdaterepresentation)canbemorecomplicated also.Nevertheless,theincreaseofthecomplexityoftheLCD generationitisnotcriticalasthisphaseisperformed independentlyfromrenderingandcannot affectthespeedofthe latter.The renderingphaseusesimplenon-intelligence algorithmandprimitiveinputdataformat(2Darraysofbytes). Soitcanbeimplementedinhardwareandperformedveryfast.

The disadvantageofLCMsisthattheyareoffinitiesize.Ifnotto useLCMsthanitispossibleto generatethetextureofany desiredsizeavoidingperiodiceffect.Besides,thesizeofinput data(thedistributiondescription)doesn'tdependonoutput imagesize.IfLCMsareused,theoutputimagecanbeofany sizealso.ButifsizeofLCMsisnotenoughtocoverthesizeof theoutputimagetheyaretobetiledandthissoonerorlaterwill leadtoperiodiceffect.ThelargertheLCMsaretheless appreciabletheperiodiceffectis.ButthelargeLCMs affectthe compactnessoftexture representation.Somecompromise betweenoutputimagequalityanddatasizeistobefound.

FirstnotethatevennotverylargeLCMscanguarantee sufficientlylargeoutputimagewithoutperiodiceffect.Indeed,if themodelconsistsoftheonlylayerandthebaseelementsizeis 32×32 pixelsthantheLCMof 64×64 entriesprovidesthe generationofanimageofsize 1024×1024 pixelswithouttiling (remindthatthedistancebetweenworeplicationpointsisone halfofbaseelementsize,hence $64(32/2) = 1024$).

Itseemsthatthesmallerthesizeofbaseelementisthelargerthe sizeofLCMmustbe.E.g.,ifthebaseelementsizeisonly 16×16 pixelsthenogenerate 1024×1024 outputimage withouttilingthesizeofLCMmustbe 128×128 .However,if themodelconsistsof atleastwolayersthereisusuallyno necessitytomakealltheLCMscovertheoutputimagesize.E.g., themodelconsistsof2layers(0and1),thebaseelementsize correspondedtolayer0is 32×32 .Then thebaseelementsize onlayer1is 16×16 pixels.Nowassumethatthesizeofboth LCMsis 64×64 andthedesiredsizeoftheoutputis 1024×1024 pixels.Thoughtilingpresentsinlayer1butwhen unitedwithlayer0,whichisfreeoftiling,thenperiodiceffectis

hardlyperceptible.Sometimesevenbetterresultscanbe achievedifLCMsizesarenotmultipliesofeachother,arenot multipliesofpoweroftwoandmaybenotsquareatall.E.g.,size oflayer0LCMis 50×60 ,sizeoflayer1LCMis 75×45 .Itis obvious thattheperiodoftheoutputismuchlargerthanthe periodofanyoftheseparatelayers.

Otherwaysofperiodiceffectdecaywithoutconsiderable increaseofrepresentationdatasizearealsoavailable.

6. DATA REPRESENTATION AND IMPLEMENTATION NOTES

Asitwasmentionedabove,theuseofLCMspermits todivide thegenerationprocessintotwophases.

The implementationdetailsofthefirstphase,theLCM generation,arenotdiscussedhere.Theonlythingcanbe mentionedisthatsincetheprobabilisticdistributionisspecified independentlyforeachlayer,thecalculationsofLCMs canbe parallelizedeasily.

Now considerthetexturerepresentationafterLCMgeneration. Obviouslyitmustbebothcompactandeasilyinterpreted.

Abaseelementisrepresentedas8-bitbitmapofspecifiedsize (inourexperimentsitwasusually 128×128 , 64×64 or 32×32 pixels).Notonlythebaseelementitselfbutalsoits copiesoflowerresolutionsaretoberepresented.Weusedtwo representationsinourexperiments.ThefirstoneisHaar transformedimage [7],whichhas exactlythesamesizeasininitial imagebutallowstoreconstructitwithanydiacresolution relativelyfast.Thesecondwayis storingallthescaledcopiesin explicitform(thisapproachissimilartomip-mapping).This requiresmorespacefor therepresentationbutprovidesmore effectiverendering(seebelow).

TherepresentationofLCMs wasdiscussed inSection 5.

Letusconsiderthe“brickwall”representationforexample.The modelconsistsof3layers:0,2and 3.Thesizeoflayer0LCMis 40×40 ,sizeoftheother(itisthesameforbothremained layers)is 20×20 .Thesizeofthebaseelementis 32×32 pixels,its 8×8 and 4×4 pixels copiesaretobestoredalso(the explicitrepresentationisconsidered).Hencetheresultis $40^2 + 20^2 + 32^2 + 8^2 + 4^2 = 3104$ bytesplusatmost20bytesfor additionalinformation(includingweightcoefficients,generation orderflag,etc.).Thisdataisenoughtogenerate texturewith period 640×640 pixels.The8-bitbitmapofthesamesize occupies409600byteswhichisapproximately130timeslarger thantheproposedrepresentation.Eveniftoadmitted resolutionlevelsofthebaseelement(16×16 and 2×2 pixels) andtousedifferentLCMsforlayers2and3thanthesizeofthe representationwillnotexceed3800byteswhichis approximately107times smallerthanthewholeimagesize.

Therepresentationcanbeevenmore compactifsome compressionmethodsareappliedtoit.Oneofthepossible approachistocodetheregularstructureofzeros(“no replication”events)inLCMs.E.g.,LCMs generated accordingto eventtables Tab. 1or Tab. 3.havemanyregularlystructured zeroentries,thus theycanbecodedinawaywhichcanreduce

the size of LCM representation approximately twice or even more. Moreover, such kind of compression can hardly affect the rendering speed. Some techniques of fast compression and decompression can be applied to base elements also.

Now let us pay attention to rendering phase and discuss the evaluation of one separate pixel of a texture.

Since almost all the data is stored in 2D arrays of bytes, access to any entry of any LCM and any pixel of any resolution level of base element is trivial. (However, if the base element is represented by its Haar transform, then additional calculations are required to get its pixels.) Given point coordinates, the rendering module can easily find entries of LCMs corresponding to specified point. Then, according to event codes, for each replication covering the point it has to evaluate corresponding pixel value. For almost all the events this evaluation consists just in finding necessary pixel in one of the scaled copies of base element, and only for "negative replication" the sign of the value is to be changed then.

For the sake of simplicity assume now that simple addition only is used for generation. According to the model definition, in any point at most four replications of the same layer can meet. So, at most 3 additions per layer are to be performed. Then obtained result is to be multiplied by weight coefficient (1 multiplication). Then values of all the N layers are to be summarized ($(N-1)$ additions) and mean intensity is to be added also (1 addition). Thus the number of operations (excluding the search of replications pixels) to render one pixel of N -layered texture doesn't exceed $4N$ additions (or similar operations) and N multiplications.

As well as for the LCM generations sufficient portion of calculations are performed independently for each layer, so it can be parallelized. Note, however, that for parallel computations scaled copies of base element are to be stored in explicit form rather than evaluated from transformed representation.

7. CONCLUSION. FURTHER WORK

The model for representation of both "abstract" and some "natural-like" scalable textures has been introduced. It was supplied with the effective generation and rendering technique. By means of this technique the most complicated calculations were encapsulated into the pre-processing phase. This permits to perform rendering phase very fast and even to implement it in hardware. The algorithm provides pixel-wise rendering, which is very important for texture-mapping purposes. The representation of texture is sufficiently compact (3-10 Kb), thus a large number of textures can be stored in graphical device memory.

Obviously, the model is not free of limitations. Sufficiently large class of objects can hardly be represented by existing variant. So the one of the tasks for further research is enhancement of the model which will enlarge the class of textures can be represented.

Another direction of further work is development of *texture analysis module* and is actually a new research project.

7.1 Model Enhancement

Some trivial enhancements of the model can make it more flexible. The "power of two" restrictions on base element size, resolution level construction and replications shifts can be weakened. On the other hand this may demand additional data for model representation and also may affect the scalability of the output.

In existing model the probabilistic distribution of events is specified independently for each layer. The opportunity to specify the distribution for neighbourhood replications on different layers can be added. But this can require synchronization between layers, which can make the LCM structures more complicated.

Some other modifications of this kind can be made also.

The more serious enhancement is implementation of more sophisticated stochastic models, models using conditional distribution, e.g., Random Markov Fields [4].

Note that the more sophisticated models used, the more complex calculations are required. But this will concern only the phase of LCM calculation, and this phase is not hardware implemented and must not be real-time. As to the rendering phase, it will work with the same (or may be slightly different) LCM structures, and thus will be as simple and fast as it is now.

7.2 Analysis Module

We assume that the structure of wider range of textures can be approximately represented in a way similar to one proposed in this paper, i.e. as a normal base elements and simple data structures controlling their replication.

One of the possible approaches is to use different modifications of wavelet transform to capture such a structure. Wavelet transform is a powerful tool for space-frequency analysis and the use of hierarchical, multi-resolution or wavelet-based methods for texture analysis is not new [1][3][5]. Moreover, the existing model has many features common with yadic 2D wavelet transform, and the use of similar methods for both synthesis and analysis seems to be promising.

8. ACKNOWLEDGEMENTS

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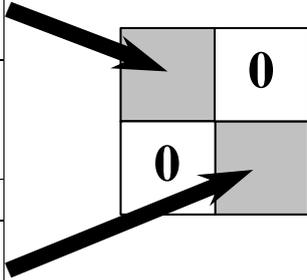
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Tab. 1. The “randomrotation” model

Pos.repl.	1.0
Neg.repl.	0.0
Norepl.	0.0
Rot.0°	0.25
Rot.90°	0.25
Rot.180°	0.25
Rot.270°	0.25
Mirroring	0.0
Addition	1.0
Non-zero	0.0
Maxinium	0.0



Tab. 2. The “simplenoise” model.

Pos.repl.	0.33
Neg.repl.	0.33
Norepl.	0.34
Rot.0°	0.25
Rot.90°	0.25
Rot.180°	0.25
Rot.270°	0.25
Mirroring	0.5
Addition	1.0

Tab. 3. The “brickwall” model.

Pos.	1.0	0	Pos.	1.0	0
0°	0.8		0°	0.2	
90°	0.05		180°	0.8	
180°	0.15		Non-z.	1.0	
Non-z.	1.0				
0	0	0	0	0	0
0	Pos.	1.0	0	Pos.	1.0
	0°	0.75		0°	0.1
	90°	0.05		90°	0.02
	180°	0.2		180°	0.88
	Non-z.	1.0		Non-z.	1.0
0	0	0	0	0	0

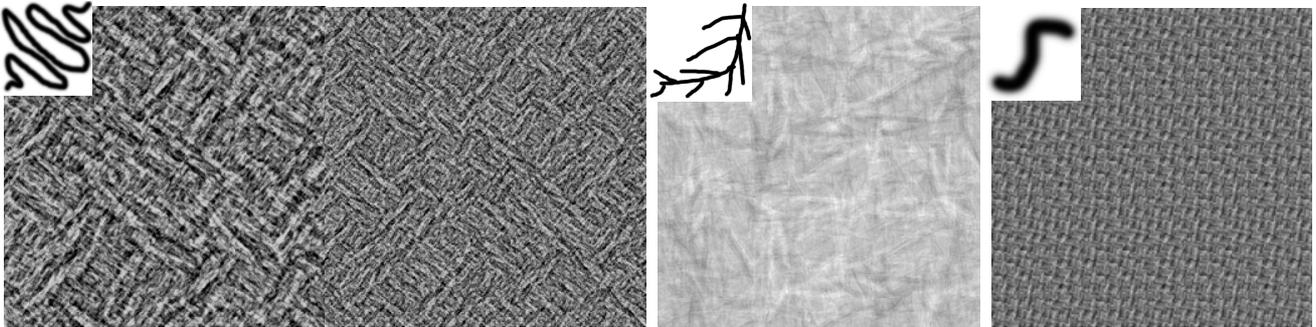


Fig. 1. Examples of “randomrotation” model.



Fig. 2. “Cheese”:baseelement and output image.

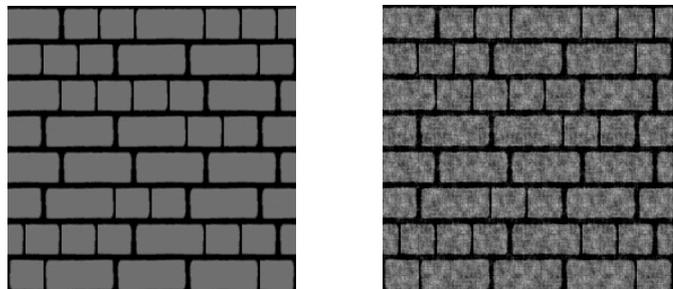


Fig. 3. “Brickwall”:baseelement, simple output image and advanced output image.